

# Safety Contracts for Timed Reactive Components

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- 1 Motivation
- 2 Contract-based Reasoning
- 3 Component framework: Timed Input/Output Automata
- 4 A toy example
- 5 Contract framework for Timed Input/Output Automata
- 6 Applying contract-based reasoning on the toy example
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## 1 Motivation

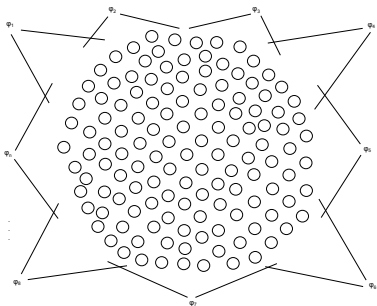
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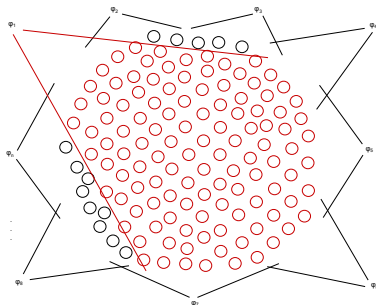
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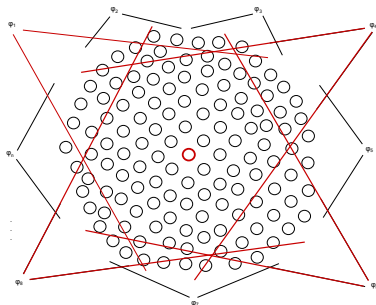


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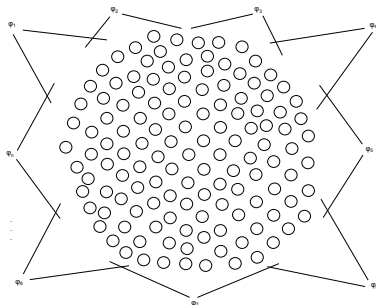


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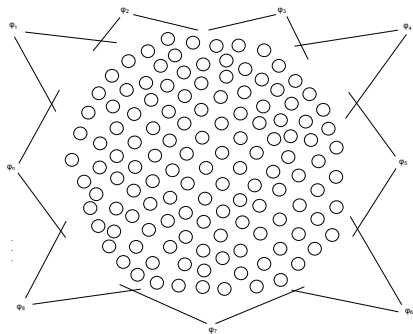
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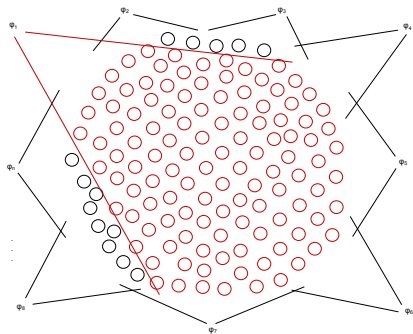
- A requirement is in general satisfied by the collaboration of a set of components
- Each component is involved in the satisfaction of several requirements  
 $\Rightarrow$  the need for **components abstractions**



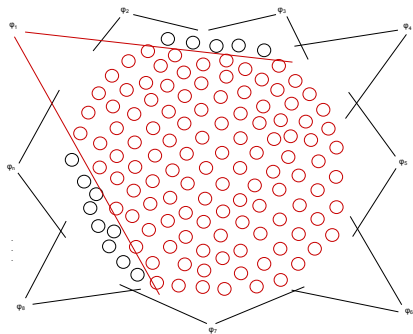
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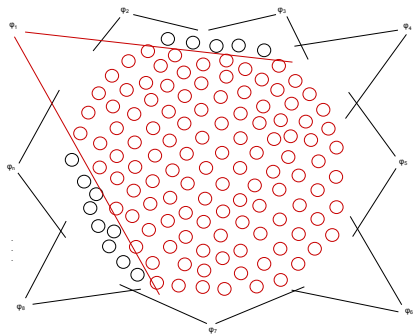
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Abstraction



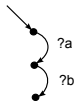
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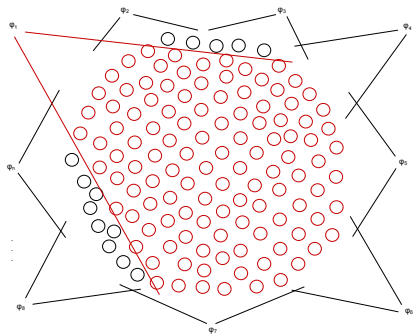
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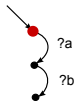
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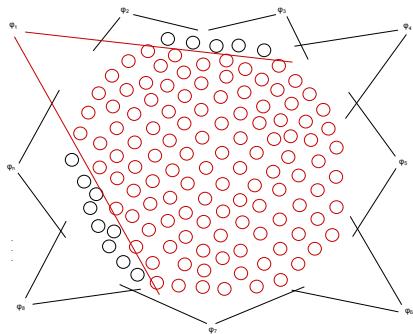
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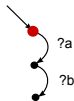
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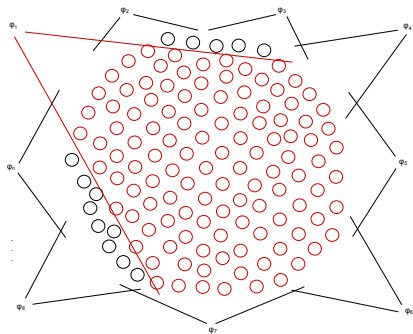


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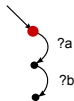


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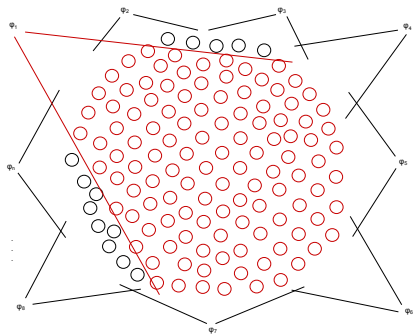


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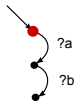


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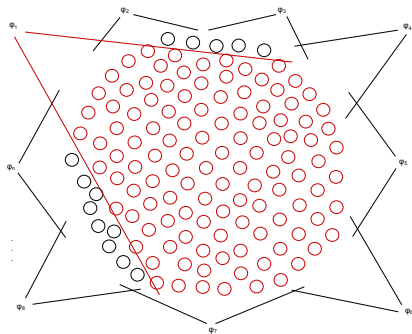
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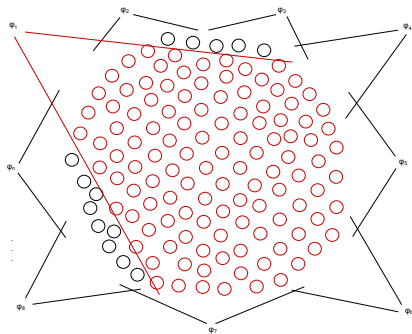


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→ usage of **contracts**

Abstraction

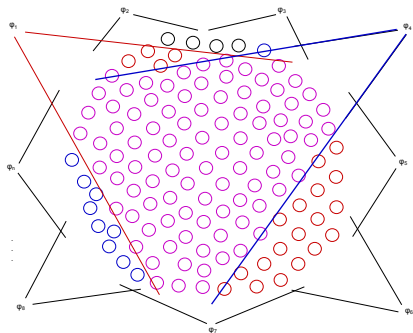


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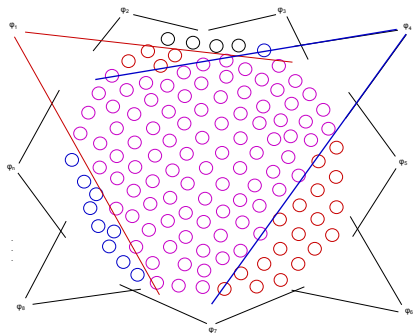
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# Introducing contracts



Contract:

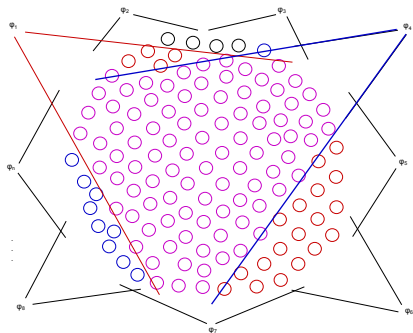
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- is a pair (*assumption*, *guarantee*)

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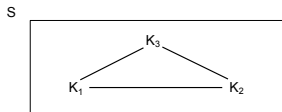


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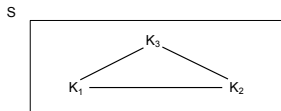
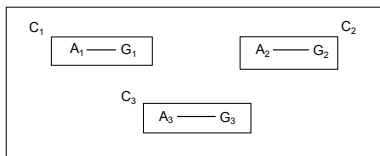
- Requirement specification and decomposition
- Mapping and tracing requirements
- Model reviews
- Verification of system designs (in SysML)

## 2 Contract-based Reasoning

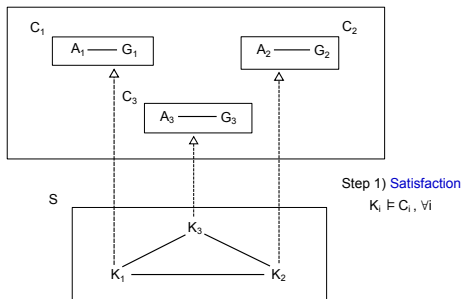
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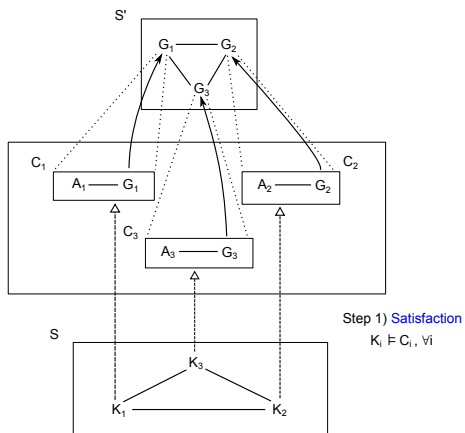
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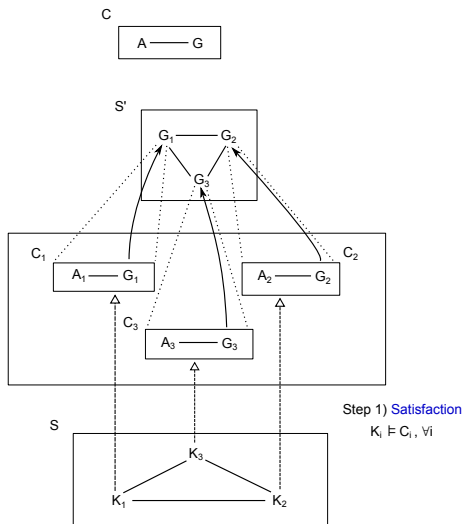
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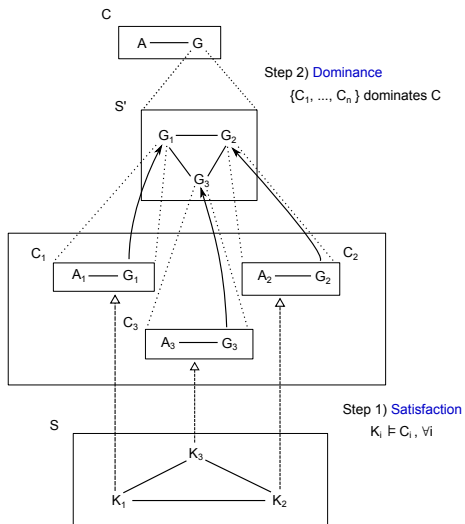
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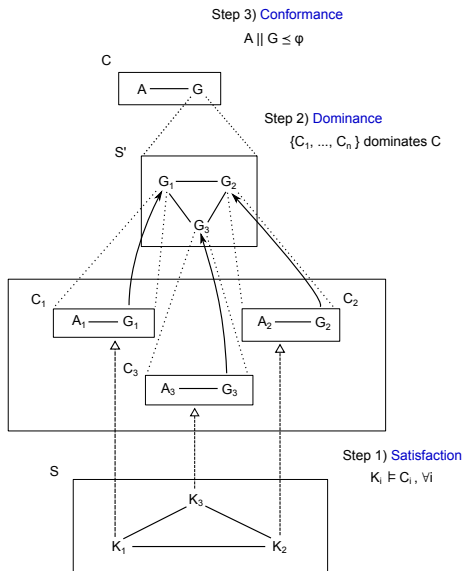


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- Formalization of component framework
- Verification relations
  - 1 Contract satisfaction
  - 2 Dominance between contracts
  - 3 Conformance

- ③ Component framework: Timed Input/Output Automata

# Component: Timed Input/Output Automaton

## Definition

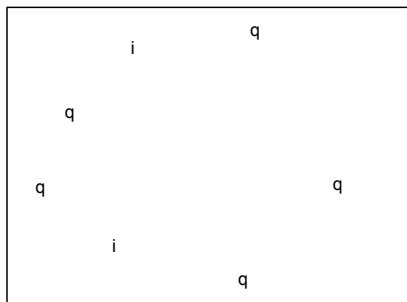
*Timed input/output automaton  $\mathcal{A}$*



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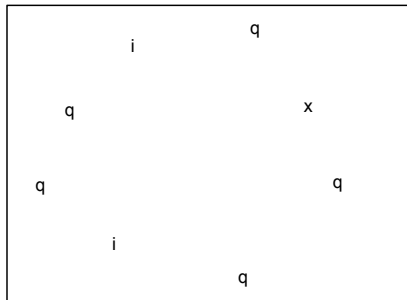
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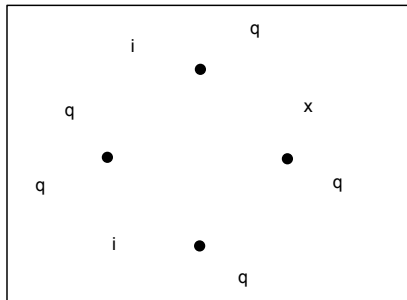




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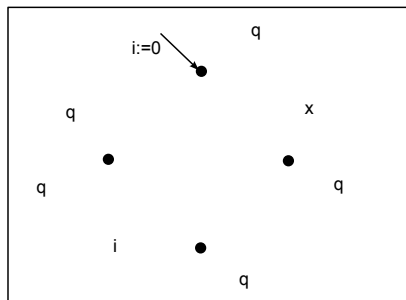
*Timed input/output automaton*  $\mathcal{A} = (X, Clk, Q,$



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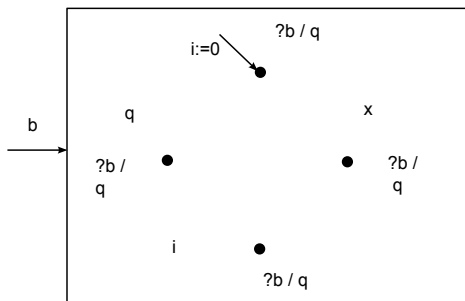
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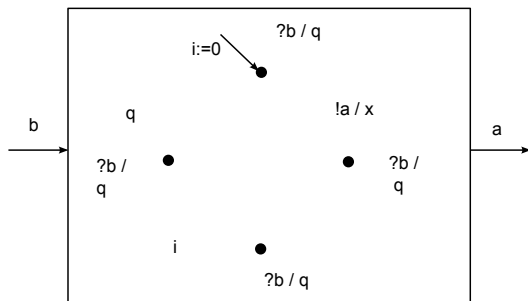
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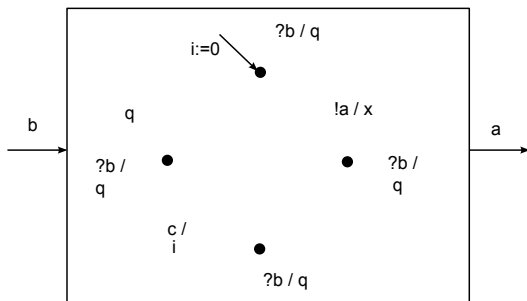
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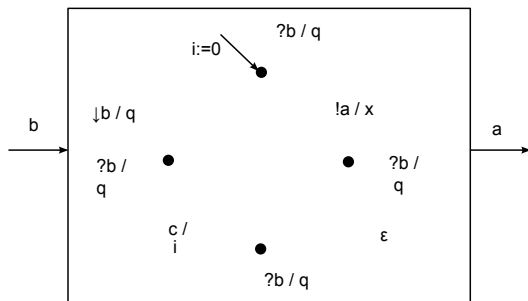
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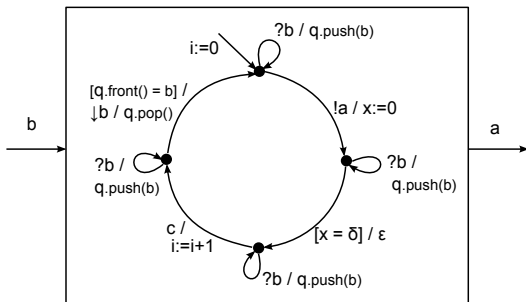
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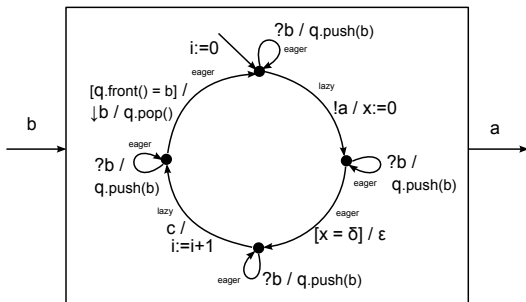
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Timed input/output automaton  $\mathcal{A} = (X, Clk, Q, \theta, I, O, V, H, D, \mathcal{T})$





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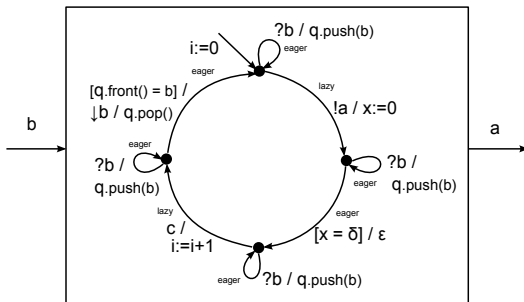
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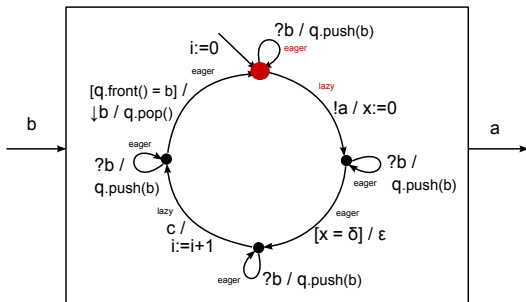
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- 4 Time-passage enabling:  $\forall x \in Q, \exists \tau \in \mathcal{T}$  such that  $\tau(0) = x$  and either
  - $\tau.limit\_time = \infty$  or
  - $\tau$  is closed and some  $l \in O \cup V \cup H$  is enabled at  $\tau(\tau.limit\_time)$

# TIOA behaviour



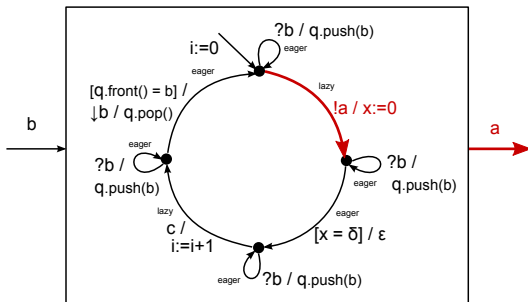
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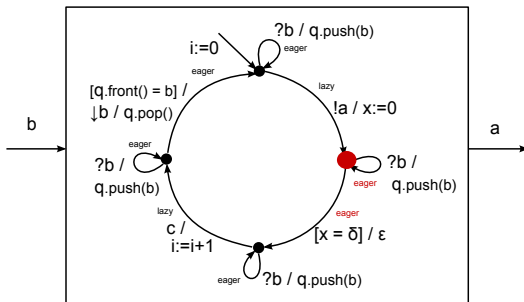
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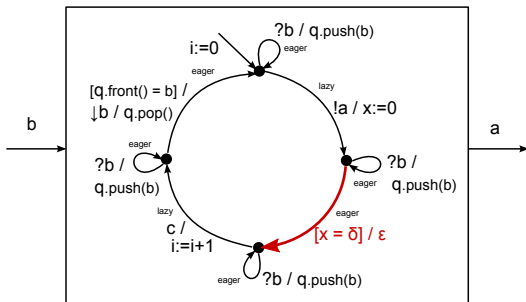
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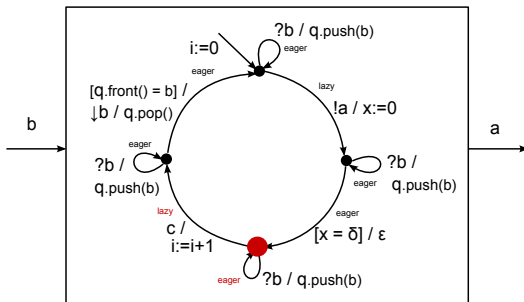


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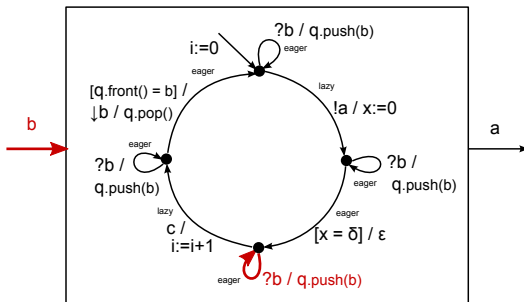
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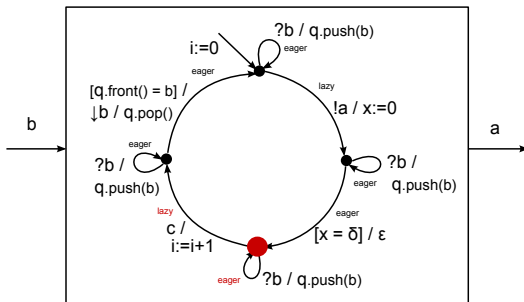
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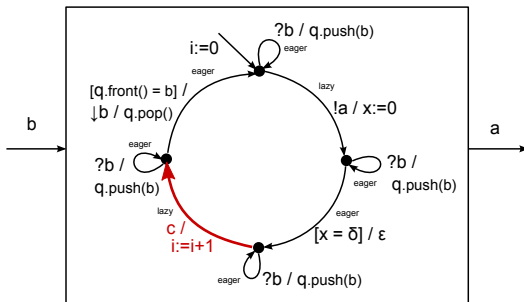
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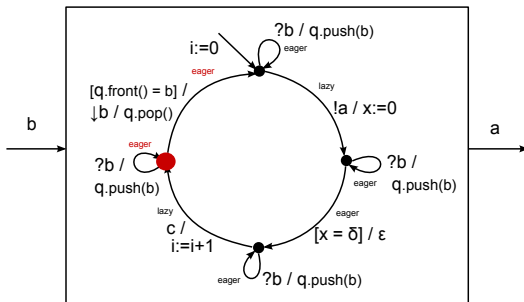
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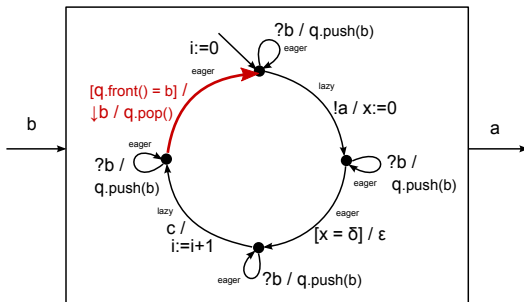
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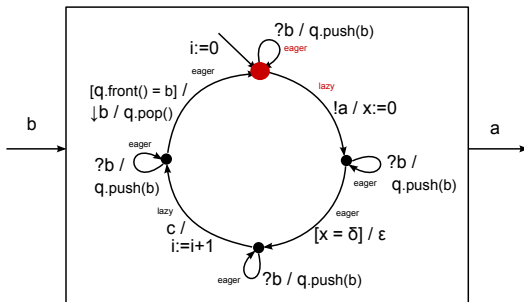
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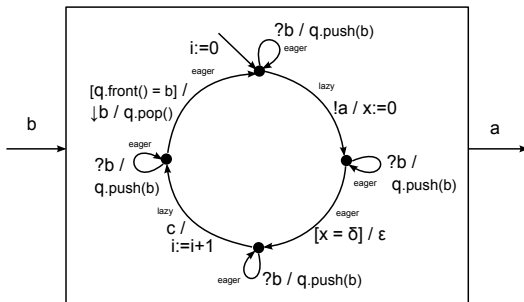
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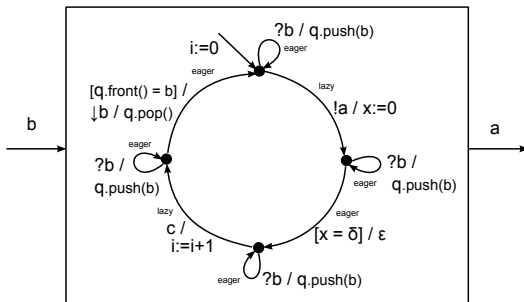


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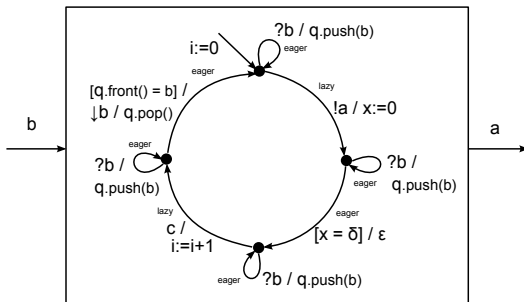
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- *Trace*: sequence of time-passage lengths and external actions  
 Example:  $trace(\alpha) =$

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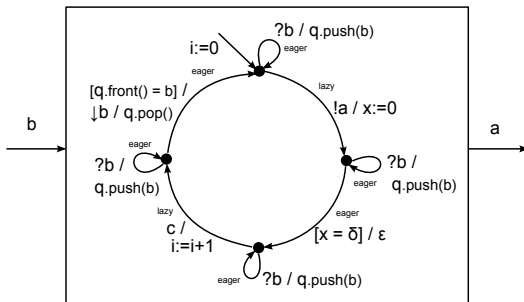
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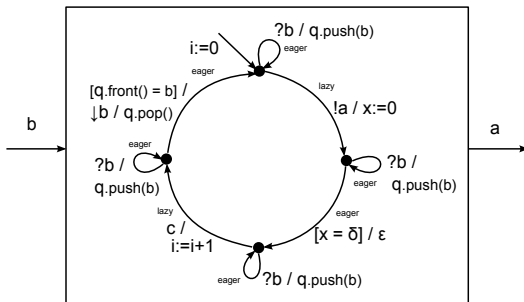
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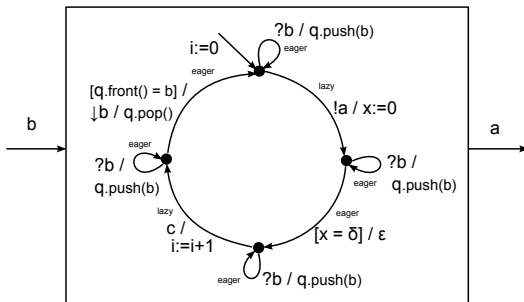
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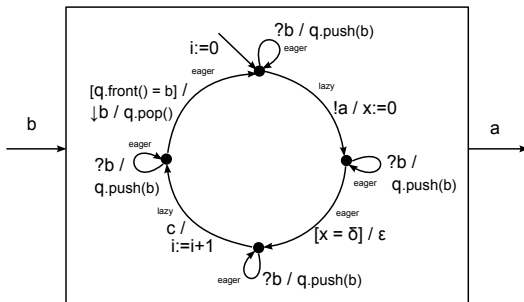
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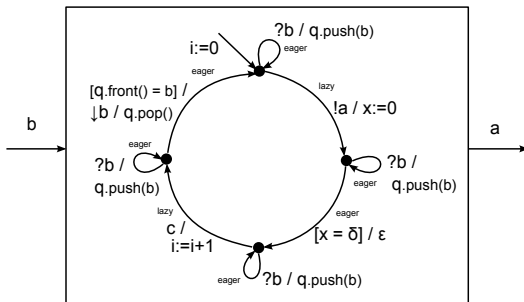
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 Example:  $\alpha = [0, 0]!a[0, \delta]\epsilon[0, \delta]?b[0, 0]c[0, 0]\downarrow b[0, 0]$
- *Trace*: sequence of time-passage lengths and external actions  
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# TIOA behaviour



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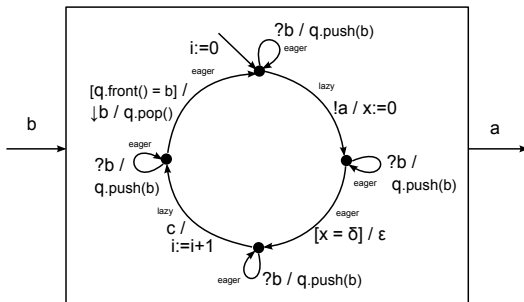
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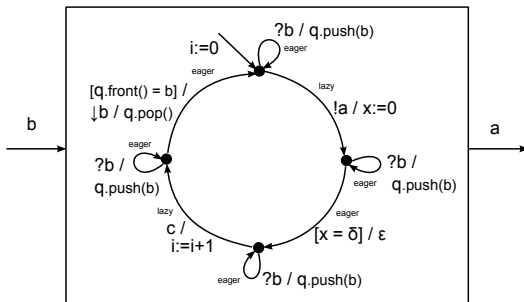


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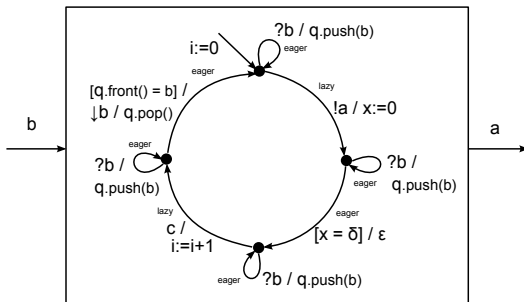
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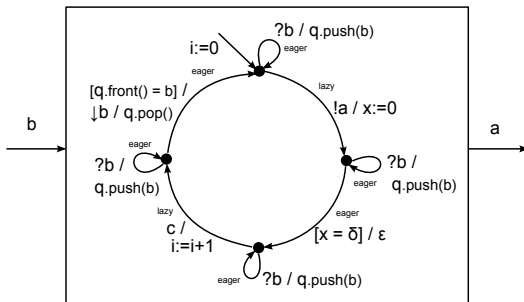
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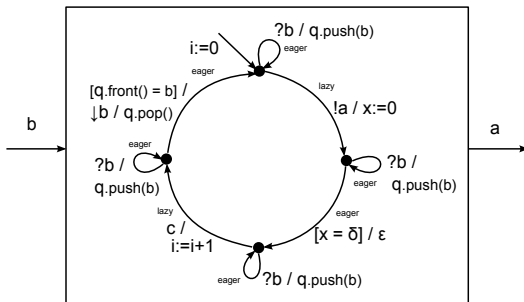
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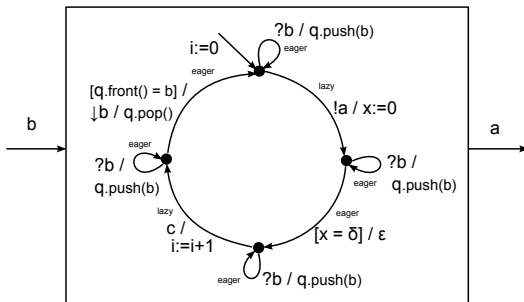
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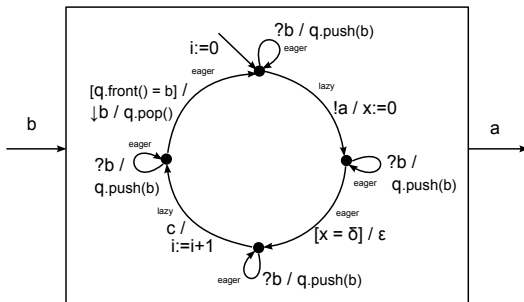
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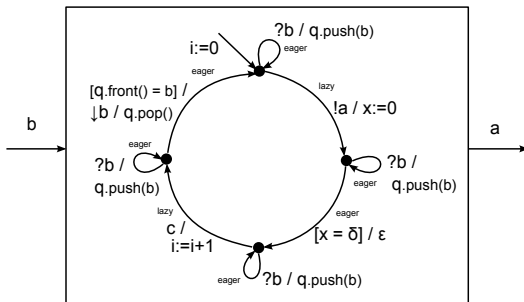
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# TIOA composition

Composition compatibility:

$$Y_i \cap Y_j = H_i \cap A_j = V_i \cap A_j = O_i \cap O_j = I_i \cap I_j = \emptyset, \text{ for } i \neq j$$

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Parallel composition:

$$\frac{x_1 \xrightarrow{a} x'_1}{(x_1 \cup x_2) \xrightarrow{a} (x'_1 \cup x_2)} (a \in A_1 \setminus A_2)$$
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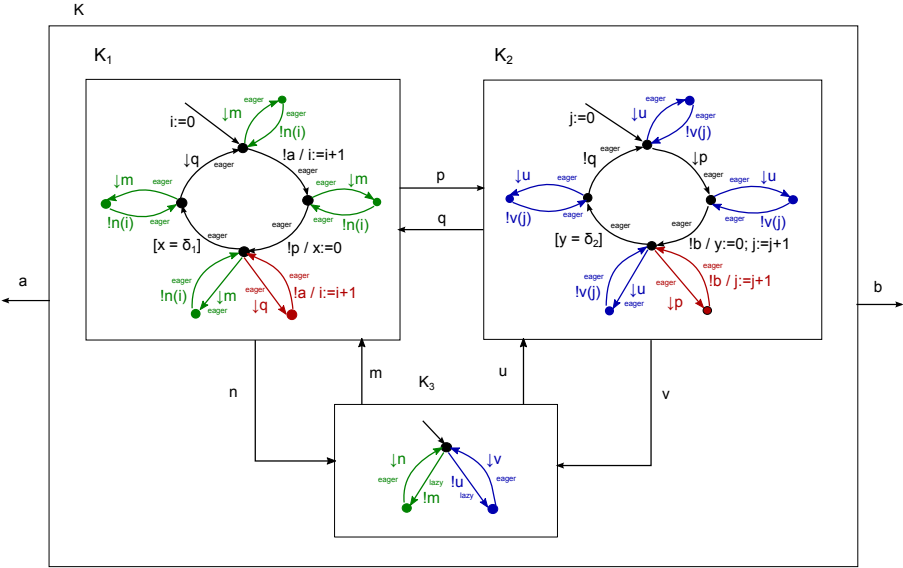
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## Theorem

The parallel composition operator is commutative and associative.

- ④ A toy example

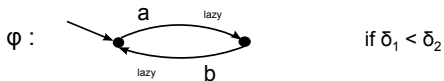
# Running example



# Property $\varphi$ to be checked

## Property

Given  $\delta_1 < \delta_2$ , the subsystem doesn't emit consecutive  $a$ 's or  $b$ 's.



- 5 Contract framework for Timed Input/Output Automata



*Component K*: a timed input/output automaton

# Formal contract

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*Closed component*:  $I = O = \emptyset$

*Open component*: it is not closed

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*Component*  $K$ : a timed input/output automaton

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*Environment*  $E$  for  $K$ : a timed input/output automaton compatible with  $K$  such that  $I_E \subseteq O_K$  and  $O_E \subseteq I_K$

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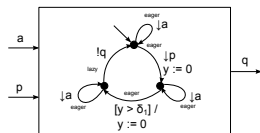
### Definition

A *contract* for a component  $K$  is a pair  $(A, G)$  of TIOA such that  $I_A = O_G$  and  $O_A = I_G$  (i.e. the composition is a closed system) and  $I_G \subseteq I_K$  and  $O_G \subseteq O_K$  (i.e. the interface of  $K$  is a refinement of that of  $G$ ).

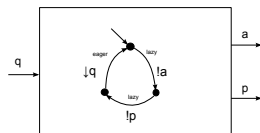
# Contracts for the running example

$C_1 = (A_1, G_1)$  contract for  $K_1$

$A_1$



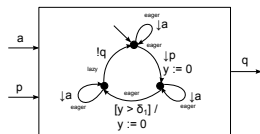
$G_1$



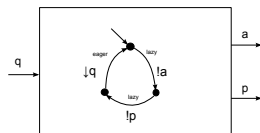
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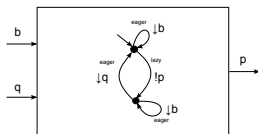


$G_1$

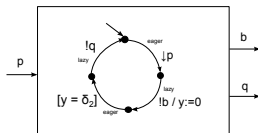


$C_2 = (A_2, G_2)$  contract for  $K_2$

$A_2$

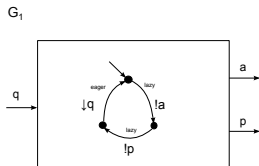
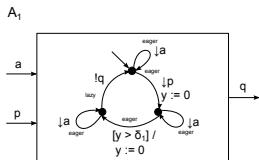


$G_2$

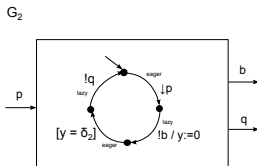
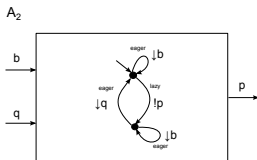


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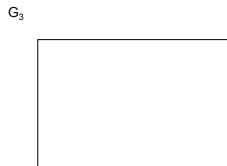
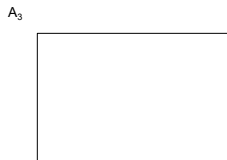
$C_1 = (A_1, G_1)$  contract for  $K_1$



$C_2 = (A_2, G_2)$  contract for  $K_2$



$C_3 = (A_3, G_3)$  contract for  $K_3$



# Conformance relation



## Definition

Let  $K_1$  and  $K_2$  be two comparable components (i.e. having the same external interface).  $K_1 \preceq K_2$  if  $traces_{K_1} \subseteq traces_{K_2}$ .

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Conformance is a preorder relation.

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Let  $K_1$  and  $K_2$  be two comparable components with  $K_1 \preceq K_2$  and  $E$  a component compatible with both  $K_1$  and  $K_2$ . Then  $K_1 \parallel E \preceq K_2 \parallel E$ .

## Refinement under context relation

### Definition

Let  $K_1$  and  $K_2$  be two components such that  $I_{K_2} \subseteq I_{K_1} \cup V_{K_1}$ ,  $O_{K_2} \subseteq O_{K_1} \cup V_{K_1}$  and  $V_{K_2} \subseteq V_{K_1}$ . Let  $E$  be an environment for  $K_1$  compatible with both  $K_1$  and  $K_2$ . We say that  $K_1$  *refines*  $K_2$  in the context of  $E$ , denoted  $K_1 \sqsubseteq_E K_2$ , if

$$K_1 \parallel E \parallel E' \preceq K_2 \parallel E \parallel K' \parallel E'$$

where  $K'$  and  $E'$  are defined such that both members of the conformance relation are comparable and closed.

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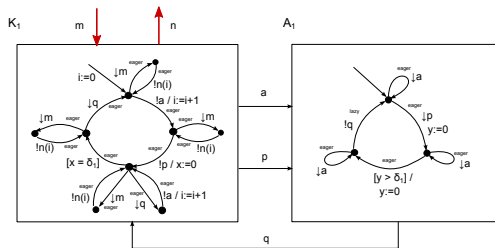
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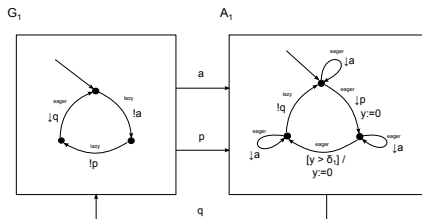
$$K \models C = (A, G) \Leftrightarrow K \sqsubseteq_A G$$

Example:  $K_1 \sqsubseteq_{A_1} G_1$

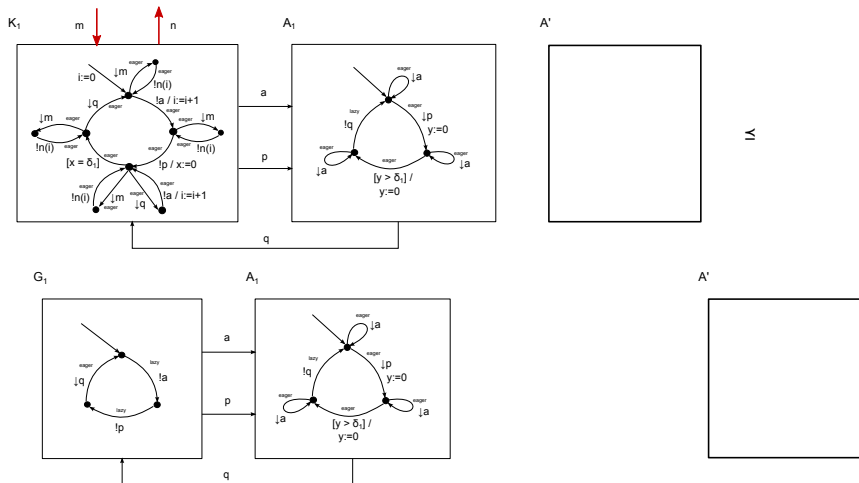
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$\gamma$

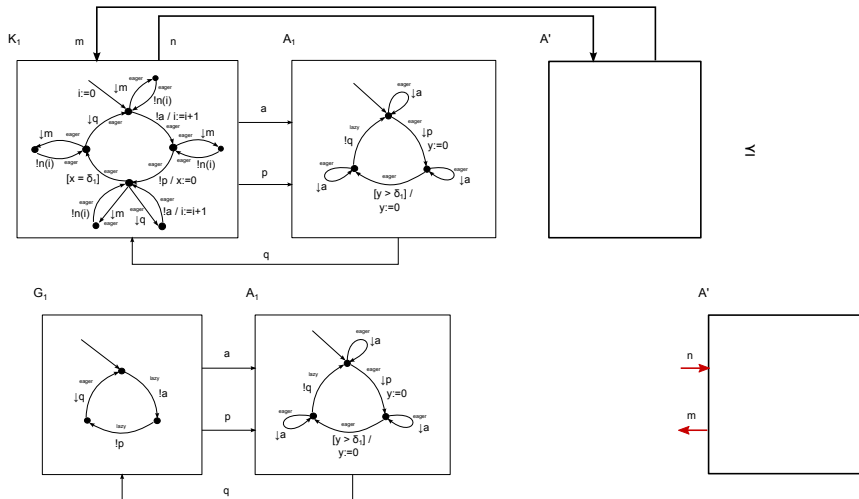


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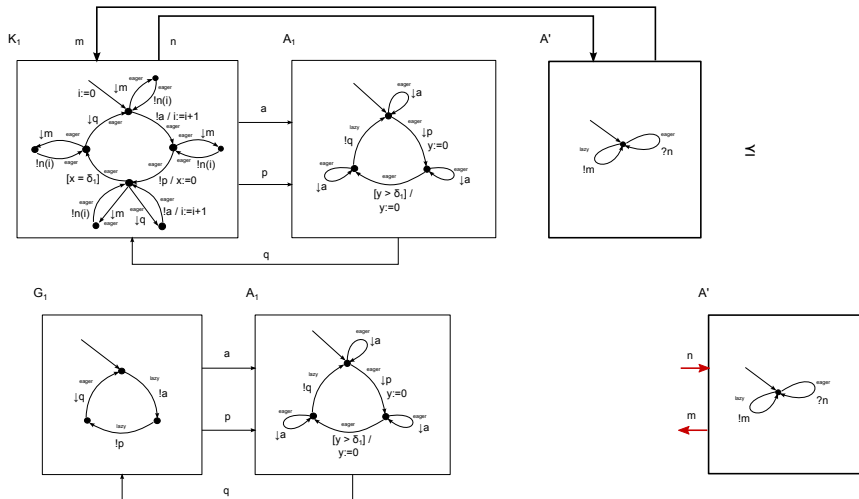




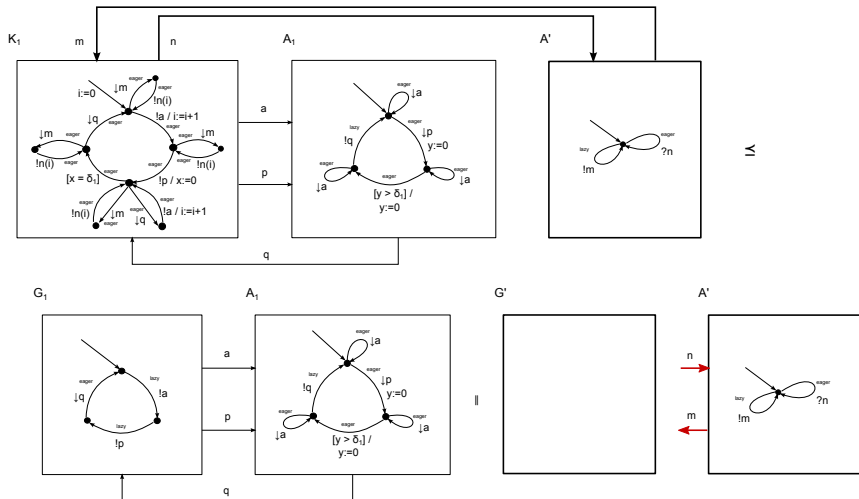
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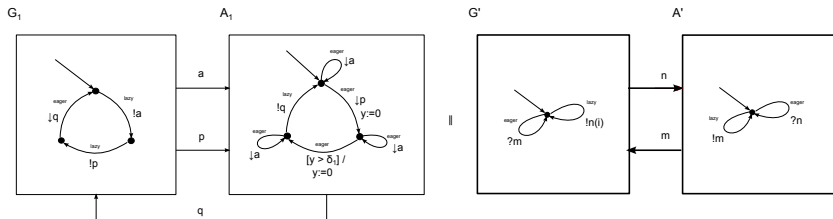
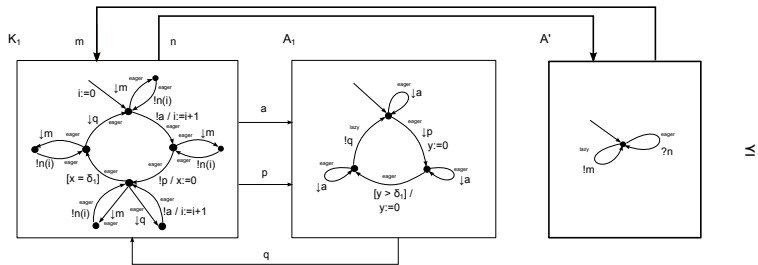
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# Properties of refinement under context

## Theorem

Given a set  $\mathcal{K}$  of comparable components and a fixed environment  $E$  for that interface, the refinement under context relation  $\sqsubseteq_E$  is a preorder over  $\mathcal{K}$ .

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### Theorem

Let  $K_1$  and  $K_2$  be two components and  $E$  an environment compatible with both  $K_1$  and  $K_2$  such that  $E = E_1 \parallel E_2$ .

$$K_1 \sqsubseteq_{E_1 \parallel E_2} K_2 \Leftrightarrow K_1 \parallel E_1 \sqsubseteq_{E_2} K_2 \parallel E_1$$

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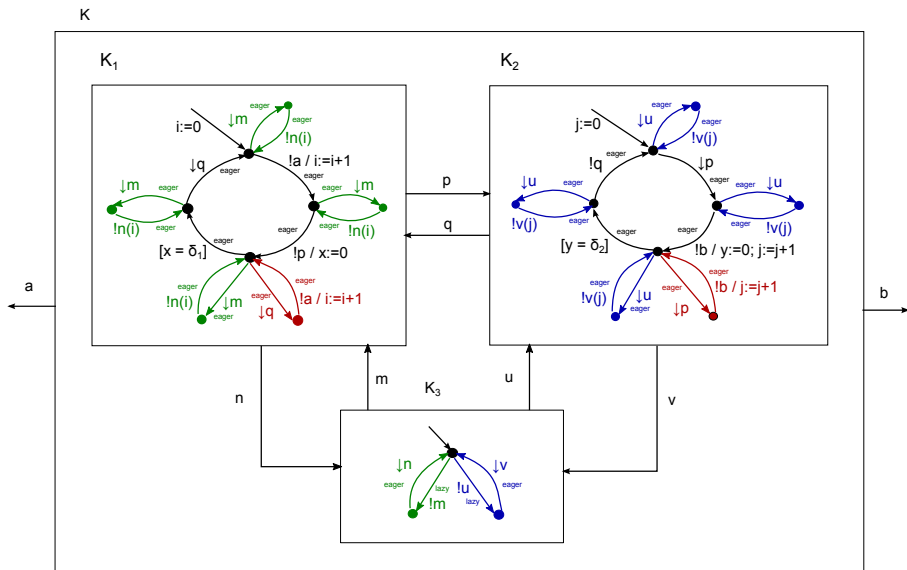
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## Theorem

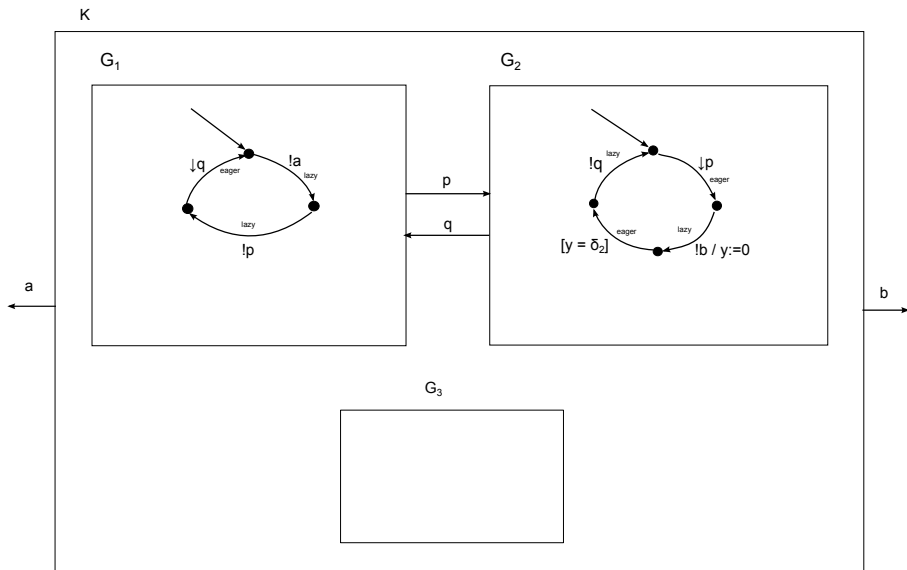
Let  $K$  be a component,  $E$  its environment and  $C = (A, G)$  the contract for  $K$  such that  $K$  and  $G$  are compatible with each of  $E$  and  $A$ . If (1)  $traces_G$  is closed under limits, (2)  $traces_G$  is closed under time-extension, (3)  $K \sqsubseteq_A G$  and (4)  $E \sqsubseteq_G A$  then  $K \sqsubseteq_E G$ .

# Abstract system



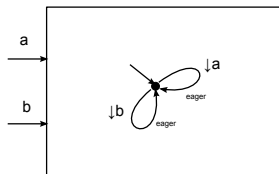


# Abstract system

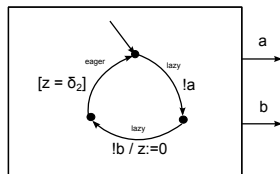


# Top contract for the abstract system

A



G



## Definition

$\{C_i\}_{i=1}^n$  *dominates*  $C$  iff  $\forall \{K_i\}_{i=1}^n$  such that,  $\forall i, K_i \models C_i$ , we have  $(K_1 \parallel K_2 \parallel \dots \parallel K_n) \models C$ .

# Contract dominance

## Definition

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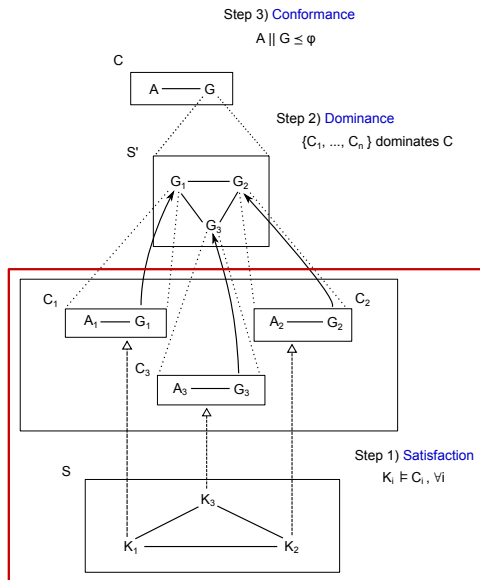
## Theorem

$\{C_i\}_{i=1}^n$  dominates  $C$  if,  $\forall i$ ,  $traces_{A_i}$ ,  $traces_{G_i}$ ,  $traces_A$  and  $traces_G$  are closed under limits and under time-extension and

$$\begin{cases} G_1 \parallel \dots \parallel G_n \sqsubseteq_A G \\ A \parallel G_1 \parallel \dots \parallel G_{i-1} \parallel G_{i+1} \parallel \dots \parallel G_n \sqsubseteq_{G_i} A_i, \forall i \end{cases}$$

- 6 Applying contract-based reasoning on the toy example

# Verifying Step 1



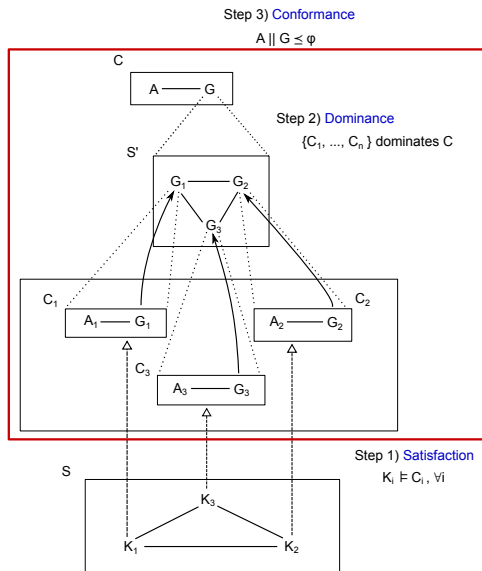
# Verifying Step 1

1  $K_1 \models C_1$

2  $K_2 \models C_2$

3  $K_3 \models C_3$

# Verifying Step 2





## Verifying Step 2

$\{C_1, C_2, C_3\}$  dominates  $C$ :

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$\{C_1, C_2, C_3\}$  dominates  $C$ :

- ①  $traces_A, traces_{A_1}, traces_{A_2}, traces_{A_3}$  are closed under limits and under time-extension
- ②  $traces_G, traces_{G_1}, traces_{G_2}, traces_{G_3}$  are closed under limits and under time-extension

## Verifying Step 2

$\{C_1, C_2, C_3\}$  dominates  $C$ :

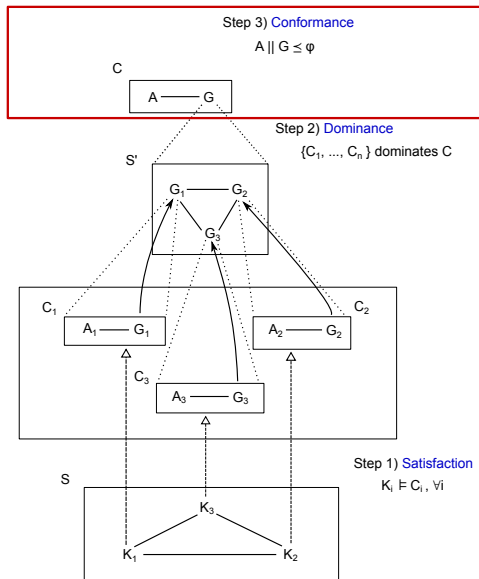
- 1  $traces_A, traces_{A_1}, traces_{A_2}, traces_{A_3}$  are closed under limits and under time-extension
- 2  $traces_G, traces_{G_1}, traces_{G_2}, traces_{G_3}$  are closed under limits and under time-extension
- 3  $G_1 \parallel G_2 \sqsubseteq_A G$

## Verifying Step 2

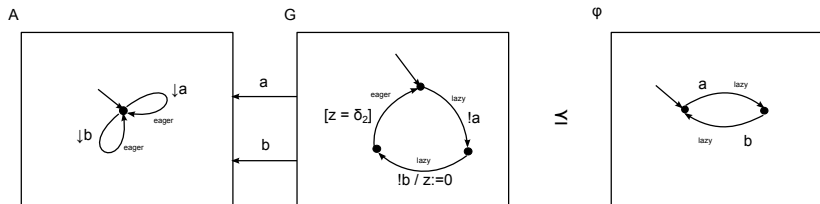
$\{C_1, C_2, C_3\}$  dominates  $C$ :

- 1  $traces_A, traces_{A_1}, traces_{A_2}, traces_{A_3}$  are closed under limits and under time-extension
- 2  $traces_G, traces_{G_1}, traces_{G_2}, traces_{G_3}$  are closed under limits and under time-extension
- 3  $G_1 \parallel G_2 \sqsubseteq_A G$
- 4  $A \parallel G_2 \sqsubseteq_{G_1} A_1$
- 5  $A \parallel G_1 \sqsubseteq_{G_2} A_2$
- 6  $A \parallel G_1 \parallel G_2 \sqsubseteq_{G_3} A_3$

# Verifying Step 3



# Verifying Step 3



## 7 Conclusions

- TIOA component framework

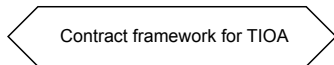


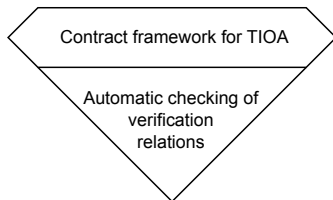
- TIOA component framework
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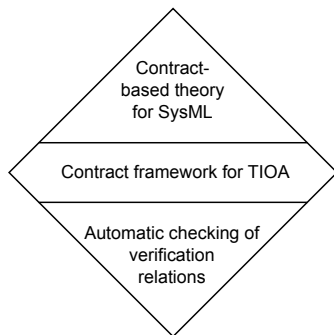
- TIOA component framework
- Formal contract with interface refinement
- Refinement relations based on *trace inclusion*
- Applied on a toy example

- (Timed) Interface Automata
- Interface Input/Output Automata
- Timed Input/Output Automata in ECDAR

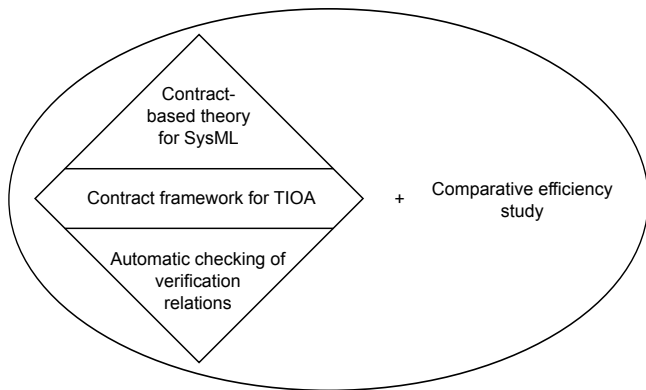




# Future work



# Future work





- 1 How to build contracts?

- 1 How to build contracts?
  - Solve for  $G$

- 1 How to build contracts?
  - Solve for  $G$
  - Automatically generate  $A$

- 1 How to build contracts?
  - Solve for  $G$
  - Automatically generate  $A$
- 2 Automation and integration within a development process

## References:

- 1 I. Dragomir, I. Ober, D. Lesens. *A Case Study in Formal System Engineering with SysML*. ICECCS 2012, Paris, 18/07/2012 - 20/07/2012, IEEE, p. 189-198, july 2012
- 2 I. Dragomir, I.Ober, C. Percebois. *Safety Contracts for Timed Reactive Systems*. Technical report, IRIT/RT-2013-11-FR, february 2013. Available at <http://www.irit.fr/~Iulian.Ober/docs/TR-Contracts.pdf>

*Thank you!*

*Any questions?*